

IV B.Tech II Semester Regular Examinations, Apr/May 2006
OPTIMIZATION OF CHEMICAL PROCESS
(Chemical Engineering)

Time: 3 hours**Max Marks: 80**

Answer any FIVE Questions
All Questions carry equal marks

1. Explain the scope and hierarchy of optimization. [16]
2. Explain the consideration of the time value of money with reference to future worth and present worth. [16]
3. For $f(x) = 3x_1^2 + 2x_1x_2 + 1.5x_2^2$ find the equation for the principal axes and determined a transformation $x = Vz$ such that $f = a_{11}z_1^2 + a_{22}z_2^2$ thus eliminating the interaction term. [16]
4. Describe in detail the basic concepts involved in linear programming? [16]
5. For a waste heat recovery system the following data are given: Cost per unit area of exchanger, $C_A = \text{Rs.}20/\text{ft}^2$
 Value of power, incorporating necessary conversion factors to have a consistent set of units, $C_H = 1.76 \times 10^{-5}$
 Average overall heat transfer coefficient, $U = 95 \text{ Btu}/(\text{h})(^\circ\text{F})(\text{ft}^2)$
 Number of hours per year of operation, $y = 8760 \text{ h/year}$
 Annualization factor for capital investment, $r = 0.365$
 Efficiency of overall system, $\eta = 0.7$
 Condensing temperature, $T_2 = 600^\circ\text{R}$
 Average hot fluid temperature, $T_s = 790^\circ\text{R}$
 Calculate the optimum value of the working fluid temperature, T_H . [16]
6. (a) What are the categories into which optimization problems for steady state distillation are classified in general? Discuss briefly.
 (b) With the help of a schematic diagram, formulate the equality constraints for optimal design and operation of a conventional staged distillation column. [8+8]
7. The cost function C representing the annual costs of a pipe line transporting a fluid is given by $C = C_1 D^{1.3} L + 0.142 (C_0/\eta) m^{2.8} m^{0.2} \rho^{-2.0} D^{-4.8} L$ where the cost coefficients are considered as $C_0 = \text{Rs.}0.59$ and $C_1 = \text{Rs.}5.7$. The mass flow rate of fluid $m = 25 \text{ kg/s}$, density $\rho = 1000 \text{ kg/m}^3$, $\mu = 1.08 \times 10^{-3} \text{ N/s m}^2$, the pumping efficiency $\eta = 0.60$ and the pipe length $L = 10 \text{ m}$. The fluid velocity is correlated by $v = 4m/(\rho \pi D^2)$ Find the optimal pipe diameter D_{opt} and optimal fluid velocity v_{opt} . [16]
8. The steady state dependence of chemostat variables, namely, cell mass concentration x and substrate concentration s are expressed by the following equations:

$$x = y_{x/s} \left(S_f - \frac{DK_s}{\mu_{\max} - D} \right)$$

$$S = \frac{DK_s}{\mu_{\max} - D}$$

where D is the dilution rate. The parameter values are: maximum specific growth rate $\mu_{\max} = 1.0 \text{ h}^{-1}$, yield factor $Y_{x/s} = 0.5$, substrate growth rate constant $K_s = 0.2 \text{ g/lit}$ and substrate feed concentration $s_f = 10.0 \text{ g/lit}$. Describe the steady state behavior of x and s as a function of D as D increases from 0 to μ_{\max} . [16]

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1. The total cost (dollars per year) for pipe line installation/operation for an incompressible fluid can be expressed by:

$$C = C_1 D^{1.5} L + C_2 m \Delta p / \rho$$

where C_1 is the installed cost of the pipe per foot length computed on an annual basis ($C_1 D^{1.5}$ is expressed in dollars per year per foot length), C_2 is based on \$ 0.05 / kWh, 365 days/year and 60 per cent pump efficiency.; D is the diameter to be optimized; L is the length of the pipe line = 100 miles; m is the mass flow rate = 200,000 lb/h; $\Delta p = 2 \rho v^2 L / (D g_c)$ f = pressure drop in psi; ρ is the density = 60 lb/ft³; v is the velocity = (4m) / ($\rho \pi D^2$); f = friction factor = $(0.046 \text{ m}^{0.2}) / (D^{\text{opt}} \text{ and } v^{\text{opt}} C^{\text{opt}})$; μ is the viscosity = 1 cP.

- (a) Find general expressions for D^{opt} , v^{opt} and C^{opt} .
- (b) For $C_1 = 0.3$ (D expressed in inches for installed cost), calculate D^{opt} and v^{opt} for the following values of μ and ρ . $\mu = 0.2, 1$ and 10 cP ; $\rho = 50, 60$ and 80 lb/ft^3 [16]
2. Discuss the important factors involved in optimizing profitability. [16]
3. Consider the following objective functions: is it convex? use eigen values in the analysis $f(x) = 2x_1^2 + 2x_1x_2 + 1.5x_2^2 + 7x_1 + 8x_2 + 24$ [16]
4. Describe in detail the basic concepts involved in linear programming? [16]
5. (a) How are capacity and economy affected in multiple effect evaporators? What is the effect of boiling point elevation on capacity? Why are multiple effects often economical?
- (b) Write about the procedure for determining the optimum number of effects in a multiple effect evaporator. [8+8]
6. (a) Discuss about the classification of optimization problems for steady state distillation.
- (b) describe how the nonlinear regression technique (least squares) can be used to fit vapor-liquid equilibrium data. Use van Laar model with two adjustable parameters to correlate the VLE data. [8+8]
7. The cost function C representing the annual costs of a pipe line transporting a fluid is given by

$$C = C_1 D^{1.3} L + 0.142 (C_0 / \eta) m^{2.8} \mu^{0.2} \rho^{-2.0} D^{-4.8} L$$

where the cost coefficients are considered as $C_0 = \text{Rs. } 0.59$ and $C_1 = \text{Rs. } 5.7$. The mass flow rate of fluid $m = 25 \text{ kg/s}$, density $\rho = 1000 \text{ kg/m}^3$, $\mu = 1.08 \times 10^{-3} \text{ N/sm}^2$, the pumping efficiency $\eta = 0.60$ and the pipe length $L = 10 \text{ m}$. Find the optimal pipe diameter D_{opt} [16]

8. The dynamic model of a continuous flow biological chemostat is given by

$$\dot{e} = \gamma k_2 c - D e$$

$$\dot{c} = k_1 s (e - c) - (k_2 + k_3) c - D c$$

$$\dot{s} = k_1 s (e - c) + (k_3 c + D(s_0 - s))$$

where e , c and s are biomass, metabolic and substrate concentrations in gmol/lit , respectively. The values of rate constants k_1 , k_2 and k_3 are 0.9 lit/mol.h , 0.7 h^{-1} and 0.0 , respectively. The limiting feed substrate concentration $s_0 = 10.0 \text{ mol/lit}$ and the parameter $\gamma = 0.09$. The dilution rate D is an independent variable. The objective is to maximize the steady state production of biomass given by $f = D e$. Obtain the steady solution of the system for $0 \leq D \leq 0.6$ and plot the responses of e , c , s and

f as a function of D . Find the value of D that provides maximum of f . [16]

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1. For a two stage adiabatic compressor, where the gas is cooled to the inlet gas temperature between stages, the theoretical work is given by :

$$W = \{k p_1 V_1 / (k - 1)\} [(p_2/p_1)^{(k-1)/k} - 1] + (p_3/p_2)^{(k-1)/k} \}$$

where $k = C_P/C_{V,1}$ $p_1 =$ inlet pressure, $p_2 =$ intermediate stage pressure,

$p_3 =$ outlet pressure and $V_1 =$ inlet volume.

We have to optimize the intermediate pressure p_2 so that the work is minimum.

Show that if $p_1 = 1 \text{ atm.}$ and $p_3 = 4 \text{ atm.}$ $p_2 \text{ opt} = 2 \text{ atm.}$ [16]

2. Describe two commonly used models of reactors along with their governing equations [16]

3. Explain the difference between uni model and multi model functions [16]

4. Use the simplex procedure with un restricted variables

minimize $f(x) = x_1 + 4x_2$

subject to $x_1 + x_2 \leq 3$

$-x_1 + x_2 \leq 1$

x_1 unrestricted, $x_2 \geq 0$

find the optimal values of x_1 and x_2 ? [16]

5. For a waste heat recovery system the following data are given: Cost per unit area of exchanger, $C_A = \text{Rs.}20/\text{ft}^2$

Value of power, incorporating necessary conversion factors to have a consistent set of units, $C_H = 1.76 \times 10^{-5}$

Average overall heat transfer coefficient, $U = 95 \text{ Btu}/(\text{h})(^\circ\text{F})(\text{ft}^2)$

Number of hours per year of operation, $y = 8760 \text{ h/year}$

Annualization factor for capital investment, $r = 0.365$

Efficiency of overall system, $\eta = 0.7$

Condensing temperature, $T_2 = 600^\circ\text{R}$

Average hot fluid temperature, $T_s = 790^\circ\text{R}$

Calculate the optimum value of the working fluid temperature, T_H . [16]

6. (a) For the determination of the optimum reflux ratio for a staged distillation column write the equality constraints with the help of a flow sheet. (Use Eduljee correlations) [6]

- (b) Develop an expression for the objective function f which is the operating profit given the following data for separating propane and propylene:

C_1 = Reboiler heat cost

C_2 = Condenser cooling cost

C_B = Value of propylene in bottoms

C'_B = Value of propane in bottoms

C_D = Value of propylene in overhead

C'_D = Value of propane in overhead

C_F = Cost per pound of propylene

C'_F = Cost per pound of propane

Q_C = Condenser load requirement

Q_R = Reboiler heat requirement

D, B, F = Distillate flow rate, Bottoms flow rate and Feed rate respectively

X_D, X_B, X_F = Mole fraction of light key in overhead, bottom and feed respectively. [10]

7. The annual costs of transporting a fluid through a pipe line depends on the diameter of the of the pipe line. The objective function for the annual costs C is a sum of annualized investment charges C_{inv} and pump operating costs C_{op} , which are expressed as

$$C_{inv} = C_1 D^{0.3} L$$

$$C_{op} = C_0 m D^p / \rho \eta$$

where C_0 and C_1 are cost coefficients, m and r are mass flow rate and density of fluid, h is pump efficiency and L is the length of pipe line. The objective function C includes four variables the pipe diameter D , the velocity v , the pressure drop Δp and the friction factor f . Three of these variables have the following correlations:

$$\Delta p = 2f \rho v^2 L / D$$

$$m = (\rho \pi D^2 / 4) v$$

$$f = (0.046 \mu^{0.2}) / (D^{0.2} v^{0.2} r^{0.2})$$

Formulate the objective function by eliminating Δp , v and f , and obtain an expression for the optimal pipe diameter D considering it as the independent variable. [16]

8. The steady state dependence of chemostat variables, namely, cell mass concentration x and substrate concentration s are expressed by the following equations:

$$x = y_{x/s} \left[s_f - \frac{DK_s}{\mu_{max} - D} \right]$$

$s = \frac{DK_s}{\mu_{max} - D}$ where D is the dilution rate. The parameter values are: maximum specific growth rate $\mu_{max} = 1.0 \text{ h}^{-1}$, yield factor $Y_{x/s} = 0.5$, substrate growth rate

constant $K_s = 0.2 \text{ g/lit}$ and substrate feed concentration $s_f = 10.0 \text{ g/lit}$. The objective is to maximize the rate of cell production Dx . show that and find the value of D_{opt} .

$$D_{opt} = \mu_{max} \left(1 - \sqrt{\frac{K_s}{K_s + s_f}} \right) \quad [16]$$

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1. Describe the general procedure for solving optimization problems, indicating the six steps used to solve optimization problems. [16]
2. Formulate net present value for a project lasting n years with an initial investment I_0 , interest rate of capital i , constant annual expense E , constant annual revenue A , salvage value S_v , yearly depreciation D_j , and a tax rate t . Compare NPV for tax rates of 0 and 50 percent, $S_v = 0$, and straight-line depreciation. Use $n = 10$ and $i = 0.15$ ($r = 0.2$). [16]
3. Consider the following objective functions: is it convex ? use eigen values in the analysis $f(x) = 2x_1^2 + 2x_1x_2 + 1.5x_2^2 + 7x_1 + 8x_2 + 24$ [16]
4. Describe in detail the basic concepts involved in linear programming? [16]
5. Develop the equation for determining the optimum number of stages and the optimal performance ratio in multiple effect evaporation. [16]
6. (a) Discuss about the classification of optimization problems for steady state distillation.
 (b) For optimal design and operation of conventional staged distillation columns formulate the equality constraints with the help of a schematic diagram. [8+8]
7. The cost function C representing the annual costs of a pipe line transporting a fluid is given by $C = C_1 D^{1.3} L + 0.142 (C_0 / \eta) m^{2.8} m^{0.2} \rho^{-2.0} D^{-4.8} L$ where the cost coefficients are considered as $C_0 = \text{Rs.} 0.59$ and $C_1 = \text{Rs.} 5.7$. The mass flow rate of fluid $m = 25 \text{ kg/s}$, density $r = 1000 \text{ kg/m}^3$, $m = 1.08 \times 10^{-3} \text{ N/sm}^2$, the pumping efficiency $\eta = 0.60$ and the pipe length $L = 10 \text{ m}$. The fluid velocity is correlated by $v = 4m / (\rho \prod D^2)$ Find the optimal pipe diameter D_{opt} and optimal fluid velocity v_{opt} . [16]
8. Apply linear programming to maximize a thermal cracker objective function represented by
 $f = 2.84x_1 - 0.22x_2 - 3.33x_3 + 1.09x_4 + 9.39x_5 + 9.51x_6$
 where x_1 = fresh ethane feed, x_2 = fresh propane feed, x_3 = gas oil feed, x_4 = DNG feed, x_5 = ethane recycle and x_6 = propane recycle.
 The objective is subjected to the following constraints:
 $1.1x_1 + 0.9x_2 + 0.9x_3 + 1.0x_4 + 1.1x_5 + 0.9x_6 \leq 200,000$
 $0.5x_1 + 0.35x_2 + 0.25x_3 + 0.25x_4 + 0.5x_5 + 0.35x_6 \leq 100,000$

$$0.01x_1 + 0.15x_2 + 0.15x_3 + 0.18x_4 + 0.01x_5 + 0.15x_6 \leq 20,000$$

$$0.4x_1 + 0.06x_2 + 0.04x_3 + 0.05x_4 - 0.6x_5 + 0.06x_6 = 0$$

$$0.1x_2 + 0.041x_3 + 0.01x_4 - 0.9x_6 = 0$$

$$x_i \geq 0$$

[16]
