

**II B.Tech I Semester Supplementary Examinations, May 2005**  
**SIGNALS & SYSTEMS**  
**(Electronics & Communication Engineering)**

Time: 3 hours

Max Marks: 70

**Answer any FIVE Questions**  
**All Questions carry equal marks**

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1. (a) Explain the importance of signal analysis with respect to communication systems and Network analysis.
- (b) Differentiate Orthogonal signal space and Orthonormal signal spaces. Discuss clearly their application with regard to representing a unknown time varying signal.
- (c) Derive the condition for orthogonality between two complex signals  $f_1(t)$  and  $f_2(t)$
2. (a) Find the Fourier series for the periodic signal shown below the figure1:

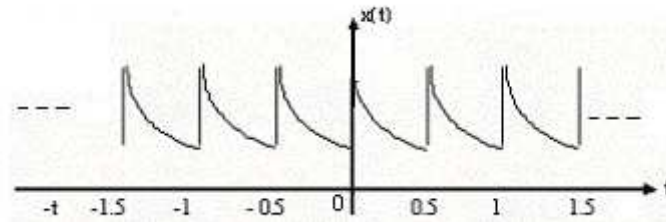


Figure 1:

- (b) With regard to Fourier series representation, justify the following statements:
  - i. Odd functions have only sine terms
  - ii. Even functions have no sine terms
  - iii. Functions with half wave symmetry have only odd harmonics.
3. (a) Determine the Fourier transform of a two sided exponential pulse  $x(t) = e^{-|t|}$
- (b) Find the Fourier transforms of an even function  $x_e(t)$  and odd function  $x_o(t)$  of  $x(t)$ .
4. (a) The transfer function of an ideal bandpass filter is given by  $H(j\omega) = k[G_w(\omega - \omega_o) + G_w(\omega + \omega_o)] \exp(-j\omega t_o)$ . Sketch the magnitude and phase function of this transfer function. Evaluate the impulse response of this filter. Sketch this response and state whether the filter is physically realizable
- (b) Derive an expression for the transfer function of an LTI system.
5. (a) A power signal  $g(t)$  has a PSD  $S_g(\omega) = N/(A^2)$   $-2\pi B \leq \omega \leq 2\pi B$  ., shown in the figure2. Where A and N are constants. Determine the PSD and the mean square value of its derivative  $d(g(t))/dt$ .

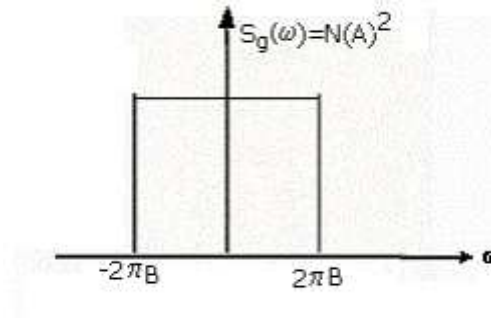


Figure 2:

- (b) Derive the relation between power and power density spectrum.
6. Determine the cross correlation function  $R_{12}(\lambda)$  of two signals  $g_1(t)$  and  $g_2(t)$  defined by
- $$g_1(t) = \begin{cases} A \cos(2\pi f_1 t + \theta_1), & 0 \leq t \leq T \\ 0, & \text{elsewhere} \end{cases} \quad g_2(t) = \begin{cases} A \cos(2\pi f_2 t + \theta_2), & 0 \leq t \leq T \\ 0, & \text{elsewhere} \end{cases}$$
- How does varying the frequency difference  $|f_1 - f_2|$  affect this cross-correlation function?
7. (a) Show the Laplace transform of  $x(t) = e^{-at} \left[ A \cos bt + \left( \frac{B - Aa}{b} \right) \sin bt \right] \cdot u(t)$  is  $X(s) = \frac{As + B}{(s^2 + 2as + c)}$  where  $c = b^2 + a^2$  and  $a > 0$ .
- (b) State and prove time-differentiation property of one-sided Laplace transform.
8. (a) State and prove the convolution and scale change properties in z transform.
- (b) Prove that the final value of  $x(n)$  for  $X(z) = z^2 / [z - 1][z - 0.2]$  is 1.25 and its initial value is unity.

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