

**III B.Tech I Semester Supplementary Examinations, April/May 2005**  
**SIGNALS AND MODULATION THEORY**  
**(Computer Science & Engineering)**

Time: 3 hours

Max Marks: 70

Answer any FIVE Questions  
 All Questions carry equal marks

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1. (a) Show that the Fourier Transform of a sine function  $y(t) = A \sin C 2\pi t$  is a gate function. Also sketch both the functions.  
 (b) Determine the energy spectral density of a square pulse  $x(t) = \Pi(t/T)$  and calculate its energy. If the signal  $x(t)$  passed through an ideal LPF of bandwidth  $f_c \text{ Hz}$ , find the energy  $E_o$  of the output  $y(t)$ .
2. (a) The auto correlation function of a random process is  $R(Z) = e^{-2\alpha|\tau|}$  determine the spectral density of the process.  
 (b) Define entropy of a
  - i. Discrete system and
  - ii. Continuous system For a discrete source producing  $m$  messages, show that the maximum value of entropy is  $H_{\max} = \log_2 m$
3. (a) Define:
  - i. Sample space and
  - ii. Random variable.

The probability density function can be written as  $p(x \leq x_j) = \sum_{K=-\infty}^j p(x_K)$

What is the interpretation of this expression.
- (b) State Central limit theorem. Discuss two examples where this theorem can be applied in detail.
4. (a) A certain random variable has a dc component of 2V and rms value of 4V. Further measurements indicate that  $\vartheta(t)$  and  $\vartheta(t - \tau)$  are independent for  $|\tau| > 5 \mu\text{sec}$  while  $R_\vartheta(\tau)$  decreases linearly with  $|\tau|$  for  $|\tau| \leq 5 \text{ msec}$ 
  - i. Plot  $R_\vartheta(t)$
  - ii. Find and plot  $G_\vartheta(t)$
- (b) Define:
  - i. Cumulative density function  $F(x)$
  - ii. Spectral density  $G(f)$  of a function.
5. (a) Draw the circuit of a FET balanced modulator and show mathematically that the circuit can act as SSB generator.
- (b) The frequency deviation in FM transmission is 25 kHz. Calculate:
  - i. Percent modulation of this signal if it is broadcast in 88.108 MHz band

- ii. Percent modulation if this signal were broadcast as audio portion of TV broadcast.
- 6. (a) With the help of waveforms, describe both the time domain and frequency domain characteristics of
  - i. Natural sampling and
  - ii. Sample-and-hold technique.
- (b) A rectangular pulse with duration  $\tau = 2$  is sampled and reconstructed using an ideal Low pass filter with  $B = f_s/2$ . Determine the output signal when  $T_s = 0.8$
- 7. (a) For a signal, the band width is 3 kHz and  $S / N = 15$ 
  - i. Calculate channel capacity
  - ii. If the bandwidth is increased to 4 kHz and signal is transmitted over same channel calculate required  $S / N$  and percentage change in signal power.
- (b) Define code efficiency A service is transmitting two symbols A and B with probabilities  $7 / 8$  and  $1 / 8$  respectively.  
Calculate the entropy of the service and required channel capacity using simplest code and also compute coding efficiency.
- 8. Write notes on:
  - (a) Convolution code
  - (b) T D Multiplexing
  - (c) Phase modulation.

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