

IV B.Tech I Semester Supplementary Examinations, April/May 2005
DIGITAL CONTROL SYSTEMS
(Electronics & Instrumentation Engineering)

Time: 3 hours**Max Marks: 70**

Answer any FIVE Questions
All Questions carry equal marks

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1. Given the transfer function $G(z) = \frac{4(z-1)(z^2+1.2z+1)}{(z+0.1)(z^2-0.3z+0.8)}$

Obtain

- (a) a series realization diagram and
- (b) a parallel realization diagram.

Using pure delay elements z^{-1} .

2. Find the state variable models for the following system represented by the difference equation

- (a) $y(k+3)+5y(k+2)+7y(k+1)+3y(k)=0$
- (b) $y(k+2)+3y(k+1)+2y(k)=5r(k+1)+3r(k)$

3. Consider the system defined by,

$$\begin{bmatrix} x_1(k+1) \\ x_2(k+1) \end{bmatrix} = \begin{bmatrix} a & b \\ c & d \end{bmatrix} \begin{bmatrix} x_1(k) \\ x_2(k) \end{bmatrix} + \begin{bmatrix} 1 \\ 1 \end{bmatrix} u(k)$$

$$y(k) = \begin{bmatrix} 1 & 0 \end{bmatrix} \begin{bmatrix} x_1(k) \\ x_2(k) \end{bmatrix}$$

Determine the condition on a, b, c and d for complete state controllability and complete observability.

4. (a) Show that the following quadratic form is positive definite.
 $V(x) = 10x_1^2 + 4x_2^2 + x_3^2 + 2x_1x_2 - 2x_2x_3 - 4x_1x_3$
- (b) State and explain Liapunov's main stability theorem.
- (c) Consider the system described by $\dot{x}_1 = x_2 - x_1(x_1^2 + x_2^2)$; $\dot{x}_2 = -x_1 - x_2(x_1^2 + x_2^2)$.
Determine the stability. Also show that $X = 0$ is the only equilibrium state.
5. (a) What are the properties of dead beat response system?
- (b) Explain in detail, how a digital controller for deadbeat performance can be obtained.
6. Consider the system given by

$$\begin{bmatrix} x_1(k+1) \\ x_2(k+2) \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ -0.16 & -1 \end{bmatrix} \begin{bmatrix} x_1(k) \\ x_2(k) \end{bmatrix} + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u(k)$$

Determine the state feedback gain matrix such that when the controls signal is given by $u(k) = -KX(k)$ the closed loop system exhibits the dead beat response to an initial state $x(0)$. Assume that the control signal $u(k)$ is unbounded.

7. (a) Discuss briefly Kalman Filtering algorithm and explain the various recursive relations.
(b) With neat block diagram explain the full order observer
8. What is a state regulator? Explain the steps involved in the design of state regulator.
