

**IV B.Tech II Semester Supplementary Examinations, April/May 2005**  
**DIGITAL CONTROL SYSTEM**  
**(Electronics & Control Engineering)**

Time: 3 hours

Max Marks: 70

Answer any FIVE Questions  
 All Questions carry equal marks

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1. (a) A slowly changing continuous-time signal  $f(t)$  is sampled every  $T$  seconds. Assuming that the changes in  $f(t)$  are very slow compared to the sampling frequency, show that in the  $z$ -domain,  $\frac{1-z^{-1}}{T}$  corresponds to differentiation. Obtain a block diagram of this differentiator using a pure delay element  $z^{-1}$ .
- (b) What is an equivalent integrator in the  $z$ -domain? Draw a graph of the output in each case when the input is a unit step sequence.
2. (a) Derive the state space model of a discrete control system using the nested programming method.
- (b) Using the above method, obtain the state equation and output equation for the system defined by  $\frac{Y(z)}{U(z)} = \frac{z^{-1}+5z^{-2}}{1+4z^{-1}+3z^{-2}}$
3. Show that the following system

$$\begin{bmatrix} x_1(k+1) \\ x_2(k+1) \\ x_3(k+1) \end{bmatrix} = \begin{bmatrix} -1 & -2 & 0 \\ 0 & -3 & 1 \\ 1 & 0 & -1 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} + \begin{bmatrix} 1 \\ 0 \\ 1 \end{bmatrix} u$$

$$y(k) = \begin{bmatrix} 1 & 1 & 0 \end{bmatrix} \begin{bmatrix} x_1(k) \\ x_2(k) \\ x_3(k) \end{bmatrix}$$

is completely state controllable and observable.

4. Explain Liapunov stability criterion for the linear time variant systems.
5. Determine which of the following digital transfer functions are physically realizable

(a)  $G(z) = \frac{10[1+0.2z^{-1}+0.5z^{-2}]}{z^{-1}+z^{-2}+1.5z^{-3}}$

(b)  $G(z) = \frac{[1.5z^{-1}-z^{-2}]}{[1+z^{-1}+2z^{-2}]}$

(c)  $G(z) = \frac{[z+1.5]}{[z^3+z^2+z+1]}$

(d)  $G(Z) = 0.1z + 1 + z^{-1}$

6. Consider an  $n^{\text{th}}$  order, single input system  $X(k+1) = AX(k) + bu(k)$  and use a feedback of the form  $u(k) = -KX(k) + r(k)$  where  $r$  is the reference input signal. Show that the zeros of the system are invariant under state feedback.

7. Consider the system

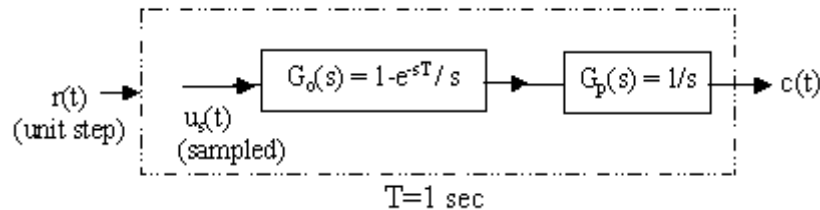
$$X(k+1) = GX(k) + Hu(k)$$

$$y(k) = CX(k)$$

$$\text{where } G = \begin{bmatrix} 0 & 0 & -0.25 \\ 1 & 0 & 0 \\ 0 & 1 & 0.5 \end{bmatrix}; H = \begin{bmatrix} 1 \\ 0 \\ 1 \end{bmatrix}; C = [1 \ 0 \ 0]$$

Assuming that the output  $y(k)$  is measurable, design a minimum-order observer such that the response to the initial observer error is deadbeat.

8. For the discrete time system shown: Find the optimal transfer function  $T^*(z)$  so



that the output  $c(t)$  follows  $r(t)$  minimizing

$$Je = \sum_{k=0}^{\infty} [r(kT) - c(kT)]^2 \text{ with } ju = \sum_{k=0}^{\infty} u^2(kT) = 0.5$$

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