

III B.Tech II Semester Supplementary Examinations,
November/December 2005

DIGITAL SIGNAL PROCESSING

(Common to Electronics & Communication Engineering, Electronics &
Instrumentation Engineering, Electronics & Control Engineering,
Electronics & Telematics and Instrumentation & Control Engineering)

Time: 3 hours

Max Marks: 80

Answer any FIVE Questions
All Questions carry equal marks

1. (a) A second order discrete time system is characterized by the difference equation. $y(n) - 0.1y(n-1) - 0.02y(n-2) = 2x(n) - x(n-1)$. Determine $y(n)$ for $n \geq 0$ when $x(n) = u(n)$ and the initial conditions are $y(-1) = -10$ and $y(-2) = 5$.

(b) State the conditions for a digital filter to be causal and stable.

[12+4]

2. Prove the following properties of the discrete Fourier series for periodic sequences.
- | Sequences | Discrete Fourier Series |
|-----------------------|-------------------------|
| (a) $x(n+m)$ | $W_N^{-Km} X(K)$ |
| (b) $x^*(n)$ | $X^*(-K)$ |
| (c) $x^*(-n)$ | $X^*(K)$ |
| (d) $\text{Re}[x(n)]$ | $X_e(K)$ |
| (e) $\text{Im}[x(n)]$ | $X_o(K)$ |

[16]

3. (a) If $x(n)$ is a periodic sequence with a period N , also periodic with period $2N$. $X_1(K)$ denotes the discrete Fourier series coefficient of $x(n)$ with period N and $X_2(k)$ denote the discrete Fourier series coefficient of $x(n)$ with period $2N$. Determine $X_2(K)$ in terms of $X_1(K)$.

(b) Prove the following properties.

i. $W_N^n x(n) \rightarrow X((K+1))_N R_N(K)$

ii. $x * (n) \rightarrow X * ((-K))_N R_N(K)$ [8+8]

4. An 8 point sequence is given by $x(n) = \{2, 2, 2, 2, 1, 1, 1, 1\}$. Compute 8 point DFT of $x(n)$ by

(a) radix - 2 D I T F F T

(b) radix - 2 D I F F F T

Also sketch magnitude and phase spectrum.

[16]

5. (a) Determine the frequency response, magnitude response and phase response for the system given by $y(n) - \frac{3}{4}y(n-1) + \frac{1}{8}y(n-2) = x(n) - x(n-1)$

- (b) A causal LTI system is described by the difference equation $y(n)=y(n-1)+y(n-2)+x(n-1)$, where $x(n)$ is the input and $y(n)$ is the output. Find
- The system function $H(Z)=Y(Z)/X(Z)$ for the system, plot the poles and zeroes of $H(Z)$ and indicate the region of convergence.
 - The unit sample response of the system.
 - Is this system stable or not? [6+10]
6. (a) Find the order and poles of a low pass Butterworth filter that has a -3db bandwidth of 500 Hz and an attenuation of 40db at 1KHz.
- (b) Convert the following analog filter with transfer function $H(S) = S + 0.1/(S + 0.2)^2 + 9$ into a digital IIR filter by using bilinear transformation method. The digital IIR filter is having a resonant frequency of $W_r = \pi/2$. [8+8]
7. (a) Compare the performances of rectangular window, hamming window and Keiser window
- (b) The desired response of a low pass filter is
- $$H_d(e^{j\omega}) = \begin{cases} e^{-j3\omega}, & -3\pi \leq \omega \leq 3\pi/4 \\ 0, & 3\pi/4 \leq |\omega| \leq \pi \end{cases}$$
- Determine $H(e^{j\omega})$ for $M=7$ using a Hamming window. [6+10]
8. (a) Describe how targets can be decided using RADAR
- (b) Give an expression for the following parameters relative to RADAR
- Beam width
 - Maximum unambiguous range
- (c) Discuss signal processing in a RADAR system. [4+6+4]

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1. (a) Let $e(n)$ be an exponential sequence $e(n) = \alpha^n$ for all 'n' and let $x(n)$ and $y(n)$ be two arbitrary sequences. Show that $[e(n)y(n)] * [e(n)x(n)] = e(n)[y(n) * x(n)]$ where '*' denotes convolution operation.
 (b) A system is described by the difference equation $y(n) - y(n-1) - y(n-2) = x(n-1)$. Assuming that the system is initially relaxed, determine its unit sample response $h(n)$.

[8+8]
2. Explain the geometrical construction method to determine magnitude and phase response of second order digital systems.

[16]
3. (a) Define DFT. Give two properties of DFT.
 (b) Discuss the effects of truncating a sequence $x(n)$ of infinite duration.
 (c) Compute the DFT of $X(n) = \{-1, 0, -1\}$ with $T = 0.5$. Plot the DFT sequence suggest a method for improving frequency resolution.

[4+6+6]
4. (a) Implement the decimation in time FFT algorithm for $N=16$.
 (b) In the above Question how many non-trivial multiplications are required.

[10+6]
5. (a) An LTI system is described by the equation $y(n) = x(n) + 0.81x(n-1) - 0.81x(n-2) - 0.45y(n-2)$. Determine the transfer function of the system. Sketch the poles and zeroes on the Z-plane.
 (b) Define stable and unstable system test the condition for stability of the first-order IIR filter governed by the equation $y(n) = x(n) + bx(n-1)$.

[8+8]
6. (a) What is an IIR digital filter?
 (b) How are IIR digital filter realized?
 (c) What are the various realizability constraints imposed on transfer function of an IIR digital filter.

[4+4+6]
7. (a) Design a low pass digital FIR filter using Kaiser window satisfying the specifications given below.
 Pass band cut-off frequency = 150 Hz.

Stop band cut-off frequency = 250 Hz.

Pass band ripple = 0.1dB

Stop band attenuation = 40 dB

Sampling frequency = 1000 Hz.

- (b) Draw the butterfly line diagram for 8 - point FFT calculation and briefly explain. Use decimation -in-time algorithm. [8+8]
8. (a) A causal system is represented by the following difference equation.
 $y(n) + \frac{1}{4}y(n-1) = x(n) + \frac{1}{2}x(n-1)$
Find the system transfer function $H(Z)$, unit sample response and frequency response of the system
- (b) Realize $H(Z) = 1 + \frac{1}{2}Z^{-1} + \frac{1}{8}Z^{-2} + \frac{3}{4}Z^{-3} + \frac{1}{8}Z^{-4} + \frac{1}{2}Z^{-5} + Z^{-6}$ with minimum number of multipliers. [8+8]

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1. By explicitly evaluating the convolution sum, evaluate the convolution $y(n) = x(n) * h(n)$ of the sequences

$$h(n) = \begin{cases} \alpha^n & 0 \leq n < N \\ 0 & \text{elsewhere} \end{cases}$$

$$X(n) = \begin{cases} \beta^{n-n_0}, & n_0 \leq n \\ 0 & , \quad n \leq n_0 \end{cases} \quad [16]$$

2. (a) Prove the modulation and time shifting properties of discrete time Fourier transform.

- (b) A discrete system is given by following difference equation

$$y(n) - 5y(n-1) = x(n) + 4x(n-1)$$

where $x(n)$ is the input and $y(n)$ is the output. Determine its magnitude and phase response as a function of frequency.

[8+8]

3. (a) Define DFT. Give two properties of DFT.

- (b) Discuss the effects of truncating a sequence $x(n)$ of infinite duration.

- (c) Compute the DFT of $X(n) = \{-1, 0, -1\}$ with $T = 0.5$. Plot the DFT sequence suggest a method for improving frequency resolution. [4+6+6]

4. (a) Draw the butterfly line diagram for 8 - point FFT calculation and briefly explain. Use decimation-in-time algorithm.

- (b) What is FFT? Calculate the number of multiplications needed in the calculation of DFT using FFT algorithm with 32 point sequence. [8+8]

5. (a) With reference to Z-transform, state the initial and final value theorem.

- (b) Determine the causal signal $x(n)$ having the Z-transform $X(Z) = \frac{Z^2+Z}{(Z-\frac{1}{2})^2(Z-\frac{1}{4})}$. [6+10]

6. (a) Using Bilinear transformation on an analog filter transfer function $H_a(S)$, given the following 'S' plane points.

$$S = 0.2 + j0, -0.1 + j0.3, -0.1 + j0.6$$

Find the corresponding 'Z' plane points. Also plot the resulting 'Z' plane points.

- (b) A signal $x(t) = 5\sin 5\pi t$ is passed through a filter. If the signal is sampled at $T=1/50$ seconds and number of sampling intervals equals 150 then sketch the input signal $x(nT)$ and the output of the filter. [8+8]
7. (a) Design a low pass filter using Fourier series method using rectangular windows for 5 taps only, if the folding frequency is 5 kHz and the corner frequencies are 1 and 3 kHz.
- (b) List the merits and demerits of Finite Impulse Response filters. [10+6]
8. (a) What are the advantages in cascade and parallel realisation of IIR systems
- (b) The transfer function of a system is given by

$$H(Z) = \frac{(1 + Z^{-1})^3}{(1 - \frac{1}{4}Z^{-1})(1 - Z^{-1} + \frac{1}{2}Z^{-2})}$$

[6+10]

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(b) State the conditions for a digital filter to be causal and stable. [12+4]
2. A LTI system is described by the difference equation $y(n) = ay(n-1) + bx(n)$. Find the impulse response, magnitude function and phase function. Find the value of b if $|H(j\omega)| = 1$. Sketch the magnitude and phase response for $a = 0.9$. [16]
3. (a) Prove the following properties.
 - i. $x^*(n) \rightarrow X^*((-K))_N R_N(K)$
 - ii. $x^*((-n))_N R_N(n) \rightarrow X_{ep}(k) = \frac{1}{2}[X((K))_N + X^*((-K))_N] R_N(K)$
 (b) Let $X(K)$ denotes the N -point DFT of the N -point sequence $x(n)$ show that if $x(n)$ satisfies the relation $x(n) = -x(N-1-n)$ then $X(0) = 0$. [8+8]
4. (a) Let $x(n)$ be a real valued sequence with N -points and Let $X(K)$ represent its DFT, with real and imaginary parts denoted by $X_R(K)$ and $X_I(K)$ respectively. So that $X(K) = X_R(K) + jX_I(K)$. Now show that if $x(n)$ is real, $X_R(K)$ is even and $X_I(K)$ is odd.
(b) Compute the FFT of the sequence $x(n) = \{1, 0, 0, 0, 0, 0, 0, 0\}$ [8+8]
5. (a) Explain how the analysis of discrete time invariant system can be obtained using convolution properties of Z transform.
(b) Determine the impulse response of the system described by the difference equation $y(n) - 3y(n-1) - 4y(n-2) = x(n) + 2x(n-1)$ using Z transform. [8+8]
6. Design a Digital IIR low pass filter with pass band edge at 1000 Hz and stop band edge at 1500 Hz for a sampling frequency of 5000 Hz. The filter is to have a pass band ripple of 0.5 db and stop band ripple below 30 db. Design Butter worth filter using both impulse invariant and Bilinear transformations. [16]
7. (a) Design a low pass filter using rectangular window by taking samples of $\omega(n)$ and with a cut-off frequency of 1.2 radians/sec.

- (b) Compare the various window functions. [8+8]
8. (a) Explain the parallel form realisation for IIR system and obtain the direct form I, direct form II realisation of the LTI systems governed by the equation.
$$y(n) = -\frac{3}{8}y(n-1) + \frac{3}{32}y(n-2) + \frac{1}{64}y(n-3) + x(n) + 3x(n-1) + 2x(n-2)$$
- (b) Compare cascade and parallel form relations. [12+4]
