

IV B.Tech. I Semester Regular Examinations, November -2005**DIGITAL SIGNAL PROCESSING
(Electrical & Electronic Engineering)****Time: 3 hours****Max Marks: 80****Answer any FIVE Questions
All Questions carry equal marks**

1. (a) For each of the following systems, determine whether or not the system is
 - i. stable
 - ii. causal
 - iii. linear
 - iv. shift-invariant.
 - A. $T[x(n)] = x(n - n_0)$
 - B. $T[x(n)] = e^x(n)$
 - C. $T[x(n)] = a x(n) + b$.

Justify your answer.
- (b) A system is described by the difference equation $y(n) - y(n-1) - y(n-2) = x(n-1)$. Assuming that the system is initially relaxed, determine its unit sample response $h(n)$.

[8+8]
2. (a) Discuss the frequency-domain representation of discrete-time systems and signals. By deriving the necessary relation.
- (b) Draw the frequency response of LSI system with impulse response $h(n) = a^n u(-n)$ ($|a| < 1$)

[8+8]
3. (a) Prove the following properties.
 - i. $x^*(n) \rightarrow X^*((-K))_N R_N(K)$
 - ii. $x^*((-n))_N R_N(n) \rightarrow X_{ep}(k) = 1/2[X((K))_N + X^*((-K))_N] R_N(K)$
- (b) Let $X(K)$ denotes the N-point DFT of the N-point sequence $x(n)$ show that if $x(n)$ satisfies the relation $x(n) = -x(N - 1 - n)$ then $X(0) = 0$.

[8+8]
4. (a) Draw the butterfly line diagram for 8 - point FFT calculation and briefly explain. Use decimation -in-time algorithm.
- (b) What is FFT? Calculate the number of multiplications needed in the calculation of DFT using FFT algorithm with 32 point sequence.

[8+8]
5. (a) With reference to Z-transform, state the initial and final value theorem.
- (b) Determine the causal signal $x(n)$ having the Z-transform $X(Z) = \frac{Z^2 + Z}{(Z - \frac{1}{2})^2 (Z - \frac{1}{4})}$.

[6+10]

6. Determine the system function $H(Z)$ of the lowest order Chebyshev digital filter that meets the following specifications.
- (a) 1 db ripple in the passband $0 \leq |W| \leq 0.3\pi$
 - (b) At least 60 db attenuation in the stopband $0.35\pi \leq |W| \leq \pi$. Use the bilinear transformation. [16]
7. (a) Design a low pass filter using rectangular window by taking samples of $\omega(n)$ and with a cut-off frequency of 1.2 radians/sec.
- (b) Compare the various window functions. [8+8]
8. (a) Describe how targets can be decided using RADAR
- (b) Give an expression for the following parameters relative to RADAR
- i. Beam width
 - ii. Maximum unambiguous range
- (c) Discuss signal processing in a RADAR system. [5+6+5]

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1. (a) The unit-sample response of a linear-shift-invariant system is known to be zero. Except in the interval $N_0 \leq n \leq N_1$. The input $x(n)$ is known to be zero except in the interval $N_2 \leq n \leq N_3$. As a result, the output is constrained to be zero except in some interval $N_4 \leq n \leq N_5$. Determine N_4 and N_5 in terms of N_0, N_1, N_2 and N_3 .
 (b) By direct evaluation of the convolution sum, determine the step response of a Linear shift-invariant system whose unit-sample response $h(n)$ is given by $h(n) = a^{-n}u(-n)$, $0 < a < 1$.

[8+8]
2. (a) Prove that the convolution in time domain leads to multiplication in frequency domain for discrete time signals
 (b) The out put $y(n)$ for a linear shift invariant system, with the input $x(n)$ is given by

$$Y(n) = x(n) - 2x(n-1) + x(n-2)$$
 Compute and sketch the magnitude and phase response of the system $|w| \leq \pi$

[8+8]
3. (a) Prove the following properties
 - i. $\arg[X(K)] = -\arg[X((-K)_N)R_N(K)]$
 - ii. $\text{Im}[X(K)] = -\text{Im}[X((-K)_N)R_N(K)]$
 (b) If $X(K)$ denotes the N-point DFT of N-Point sequence $x(n)$, show that with N even and if $x(n) = x(N-1-n)$ then $X(N/2) = 0$.

[8+8]
4. (a) Let $x(n)$ be a real valued sequence with N-points and Let $X(K)$ represent its DFT, with real and imaginary parts denoted by $X_R(K)$ and $X_I(K)$ respectively. So that $X(K) = X_R(K) + jX_I(K)$. Now show that if $x(n)$ is real, $X_R(K)$ is even and $X_I(K)$ is odd.
 (b) Compute the FFT of the sequence $x(n) = \{1, 0, 0, 0, 0, 0, 0, 0\}$

[8+8]
5. (a) With reference to Z-transform, state the initial and final value theorem.
 (b) Determine the causal signal $x(n)$ having the Z-transform $X(Z) = \frac{Z^2+Z}{(Z-\frac{1}{2})^2(Z-\frac{1}{4})}$.

[6+10]
6. Design a low pass digital filter with the following specifications;
 Maximum pass band attenuation $\alpha_{max} = -3\text{db}$, for $0 \leq w \leq 2\pi/10$

Minimum stop band attenuation $\alpha_{max} = -15db$, for $3\pi/10 \leq w \leq \pi$

Use following two methods:

- (a) Impulse invariance method
- (b) Bilinear transformation method.

Assume $T = 0.2$ msec. [16]

7. Design a low pass Finite Impulse Response filter that approximate the following frequency response:

$$H(f) = \begin{cases} 1; & 0 \leq f \leq 1000 \text{ Hz} \\ 0; & \text{elsewhere in the range } 0 \leq f \leq f_s/2 \end{cases}$$

when the sampling frequency is 8000 sps. The impulse response duration is to be limited to 2.5 msec. Draw the filter structure. [16]

8. (a) How is a speech signal generated?
(b) Give the model of human speech production system and explain. [6+10]

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1. By explicitly evaluating the convolution sum, evaluate the convolution $y(n) = x(n) * h(n)$ of the sequences

$$h(n) = \begin{cases} \alpha^n & 0 \leq n < N \\ 0 & \text{elsewhere} \end{cases}$$

$$X(n) = \begin{cases} \beta^{n-n_0}, & n_0 \leq n \\ 0, & n \leq n_0 \end{cases} \quad [16]$$

2. (a) Let $x_1(n) = x_2(n) = \begin{cases} 1 & 0 \leq n \leq N-1 \\ 0 & \text{otherwise} \end{cases}$

Find out the circular convolution of these sequences.

- (b) If $x_1(n)$ and $x_2(n)$ are two finite sequences, derive the linear convolution of these sequences. Using circular convolution.

[8+8]

3. (a) Define DFT. Guide two properties of DFT.
 (b) Discuss the effects of truncating a sequence $x(n)$ of infinite duration.
 (c) Compute the DFT of $X(n) = \{-1, 0, -1\}$ with $T = 0.5$. Plot the DFT sequence suggest a method for improving frequency resolution. [4+6+6]

4. (a) Implement the decimation in time FFT algorithm for $N=16$.
 (b) In the above Question how many non-trivial multiplications are required. [10+6]

5. (a) Explain how the analysis of discrete time invariant system can be obtained using convolution properties of Z transform.
 (b) Determine the impulse response of the system described by the difference equation $y(n) - 3y(n-1) - 4y(n-2) = x(n) + 2x(n-1)$ using Z transform. [8+8]

6. Determine the system function $H(Z)$ of the lowest order Chebyshev and Butterworth digital filter with the following specification

- (a) 3 db ripple in pass band $0 \leq w \leq 0.2\pi$
 (b) 25 db attenuation in stop band $0.45\pi \leq w \leq \pi$ [16]

7. (a) Design a high pass filter using hamming window with a cut-off frequency of 1.2 radians/second and $N=9$
 (b) Compare FIR and IIR filters. [10+6]

8. (a) Explain the parallel form realisation for IIR system and obtain the direct form I, direct form II realisation of the LTI systems governed by the equation.
$$y(n) = -\frac{3}{8}y(n-1) + \frac{3}{32}y(n-2) + \frac{1}{64}y(n-3) + x(n) + 3x(n-1) + 2x(n-2)$$
- (b) Compare cascade and parallel form relations. [12+4]

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1. (a) Consider a LSI system with unit sample response $h(n)$ where $h(n) = \alpha^n u(n)$ where α is real and $0 < \alpha < 1$. If the input is $x(n) = \beta^n u(n)$, $0 < |\beta| < 1$, determine the output $y(n)$ in the form $y(n) = (k_1 \alpha^n + k_2 \beta^n) u(n)$ by explicitly evaluating the convolution sum.
- (b) Define causality and stability of LSI system and state the conditions for stability.

[12+4]

2. (a) Prove the modulation and time shifting properties of discrete time Fourier transform.
- (b) A discrete system is given by following difference equation
 $y(n) - 5y(n-1) = x(n) + 4x(n-1)$
 where $x(n)$ is the input and $y(n)$ is the output. Determine its magnitude and phase response as a function of frequency.

[8+8]

3. (a) State and prove the circular time shifting and frequency shifting properties of the DFT.
- (b) Compute the circular convolution of the sequences
 $x_1(n) = \{1, 2, 0, 1\}$ and
 $x_2(n) = \{2, 2, 1, 1\}$ Using DFT approach.

[8+8]

4. (a) Implement the decimation in time FFT algorithm for $N=16$.
- (b) In the above Question how many non-trivial multiplications are required.

[10+6]

5. (a) With reference to Z-transform, state the initial and final value theorem.
- (b) Determine the causal signal $x(n)$ having the Z-transform $X(Z) = \frac{Z^2 + Z}{(Z - \frac{1}{2})^2 (Z - \frac{1}{4})}$.

[6+10]

6. (a) Compare Butterworth and Chebyshev approximations.
- (b) Determine the order and transfer function of the Chebyshev filter for following specifications:
 - i. Maximum pass band ripple is 1 db for $\Omega \leq 4$ rad/sec.
 - ii. Stop band attenuation is 40 db for $\Omega \geq 4$ rad/sec.

[8+8]

7. (a) Design a Finite Impulse Response low pass filter with a cut-off frequency of 1 kHz and sampling rate of 4 kHz with eleven samples using Fourier series method.
(b) Show that an FIR filter is linear phase if $h(n) = h(N-1-n)$. [8+8]
8. (a) Explain in detail the short time Fourier analysis for speech signals
(b) What is a vocoder? Explain with a block diagram. [10+6]
