

III B.Tech I Semester Supplementary Examinations, November 2006
GAS DYNAMICS
(Aeronautical Engineering)

Time: 3 hours

Max Marks: 80

Answer any FIVE Questions
 All Questions carry equal marks

1. Derive the energy equation [16]

$$\frac{a^2}{r-1} + \frac{1}{2}C^2 = \frac{1}{2}C_{\max}^2 = \frac{a_0^2}{r-1} = L_0$$
 Stating the assumptions used
 An air jet ($r = 1.4$, $R=287$ J/kg K) at 400K has sonic velocity. Determine
 - (a) Velocity of sound at 400K
 - (b) Velocity of sound at the stagnation condition
 - (c) Maximum velocity of the jet
 - (d) Stagnation enthalpy
 - (e) Crocco Number.

2. (a) Explain briefly the following terms [2 × 5]
 - i. Control volume
 - ii. Internal energy and enthalpy
 - iii. II^{nd} law of thermodynamics
 - iv. Adiabatic and isentropic process
 - v. Non-flow process
 (b) Define stagnation enthalpy and stagnation temperature. Do these quantities define the stagnation state. [6]

3. Describe the behaviour of flow in a convergent divergent nozzle when it is operated at [16]
 - (a) Design pressure ratio
 - (b) Pressure ratio higher than design value and
 - (c) Pressure ratio lower than the design value

4. The ratio of the exit to entry area in a subsonic diffuser is 4.0. The mach number of a jet of air approaching the diffuser at $p_0 = 1.013\text{bar}$, $T=288$ is 2.3. There is standing a normal shock wave just outside the diffuser entry. The flow in the diffuser is isentropic. Determine at the exit of the diffuser. [16]
 - (a) Mach number
 - (b) Temperature and
 - (c) Pressure

5. (a) Show that the Mach number downstream of the normal shock wave is given by

[2 × 8]

$$My^2 = \frac{\frac{2}{r-1} + M_x^2}{\frac{2r}{r-1} M_x^2 - 1}$$

M_x = Upstream Mach number

- (b) Explain how strong compression and expansion waves are formed in a compressible fluid.
6. A combustion chamber in a gas turbine plant receives air at 320 K, 0.5 bar and 70m/s. The air fuel ratio is 27 and calorific value of the fuel is 40.87MJ/Kg. Taking $r=1.4$ and $R=0.287\text{KJ/kg K}$ for the gas. determine [16]
- (a) The initial and final Mach number
- (b) Final pressure, temperature and velocity of the gas
- (c) Percent stagnation pressure loss in the combustion chamber and
- (d) The maximum stagnation temperature attainable.
7. Derive the following Equation for Fanno flow. [16]

$$(a) \frac{C}{C^*} = \frac{\rho^*}{\rho} = \left[\frac{(r+1)M^2}{2+(r-1)M^2} \right]^{1/2}$$

$$(b) \left(\frac{4\bar{f}L_{\max}}{D} \right)_M = \frac{1-M^2}{rM^2} + \frac{r+1}{2r} \ln \frac{(r+1)M^2}{2+(r-1)M^2}$$

8. Explain what is Prandtl-Meyer angle? Starting from flow geometry show that the value of Prandtl-Meyer angle is [16]

$$W(M) = \int \frac{\sqrt{M^2 - 1}}{2M^2 \left(1 + \frac{r-1}{2} M^2 \right)}$$

Also obtain the value of the above integral and show that the maximum Prandtl-Meyer angle is

$$\left(\sqrt{\frac{r+1}{r-1}} - 1 \right) \frac{\Pi}{2} = 130.5^\circ (\text{for } r = 1.4)$$
